“Clean Up” of Oil Zones after a Gel Treatment
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Also see SPE paper 92772

- Mature oil wells typically produce >7 bbls water per bbl of oil.
- Polymer solutions and gels are often placed in oil production wells to try to reduce water production.
- Polymers and gels usually enter both oil and water strata when placed.

**ABSTRACT**

Because polymers and gels can reduce permeability to water much more than that to oil, an unfavorable displacement (high mobility ratio) usually occurs in oil zones when wells are returned to production after bull-headed gel treatments. Since oil displacement through gel is unfavorable, the permeability to oil requires a large throughput to stabilize. Consequently, oil zones often exhibit a significant “clean-up time” after field applications of gel treatments. The oil and water throughput requirements for stabilization of permeabilities were studied for a relatively “strong” pore-filling Cr(III)-acetate-HPAM gel and for a “weak” adsorbing polymer. As oil throughput increased from 1 to 100 PV, permeability to oil gradually increased by factors from 5 to 10 for cores treated with the Cr(III)-acetate-HPAM gel and from 2 to 3 for cores treated with the adsorbing polymer. In contrast, after treatment with gel, permeability to water stabilized rapidly and remained very low for over eight months. An explanation is provided. We also noted that a minimum pressure gradient was required for oil to initiate flow through a gel bank (1.3-1.7 psi/ft for our Cr(III)-acetate-HPAM gel in an 8-darcy core).
A simple displacement model was used to predict clean-up times for both fractured and unfractured wells after a gel treatment. The time to restore productivity to a gel-treated oil zone (1) was similar for radial versus linear flow, (2) varied with the cube of distance of gel penetration, (3) varied inversely with pressure drawdown, (4) varied inversely with the $k_w$ at $S_{wr}$ in the gel-treated region, and (5) was not sensitive to the final $k_o$ at $S_{sw}$. Although $k_o$ at $S_{sw}$ (after gel placement) had no effect on the clean-up time, it strongly affected how much of the original oil productivity was ultimately regained. Earlier work demonstrated that an acceptable gel or polymer placement can be achieved by unrestricted injection of gelants during linear flow (e.g., vertically fractured wells). However, in radial flow through matrix (e.g., unfractured wells), hydrocarbon productive zones must be protected during gelant or polymer placement. These conclusions were confirmed by our new results for both the Cr(III)-acetate-HPAM gel and the adsorbing polymer.

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Introduction

Utility of Disproportionate Permeability Reduction. In mature reservoirs, wells typically produce more water than hydrocarbon. In many wells, hydrocarbon productivity could be increased significantly if the water production rate could be reduced. For these cases, the water and hydrocarbon must flow to the wellbore through different pathways (i.e., some zones have high fractional hydrocarbon flow, while other zones have high fractional water flow).\textsuperscript{1} Because of physical or economic constraints, remedial chemical treatments (e.g., gel treatments) that are intended to plug water strata are often placed without zone isolation. Consequently, the injected fluids and chemicals penetrate into both hydrocarbon and water zones, and the operator must be concerned about damage to hydrocarbon productivity.\textsuperscript{1,2} Certain water-based gels and water-soluble polymers (after adsorption or entrapment in rock) can reduce permeability to water much more than that to hydrocarbon.\textsuperscript{3,4} Basic engineering calculations reveal that materials that provide “relative permeability modification” (RPM) or “disproportionate permeability reduction” (DPR) are currently of far more practical use when treating linear flow features (e.g., fractures) than when treating radial matrix flow problems (e.g., wells without fractures).\textsuperscript{5-7} For these materials to effectively treat radial matrix flow, they should reduce permeability to water by more than a factor of 10 (and preferably by more than a factor of 20). At the same time, they must reduce permeability to oil by less than a factor of two if oil zones are not protected during placement.\textsuperscript{5}
In contrast, when treating fractures, a significant oil residual resistance factor (permeability reduction value for oil) can be tolerated so long as (1) the permeability to water is reduced much more (e.g., >50 times more) than that to oil and (2) the distances of gelant leakoff from the fracture faces are controlled.\textsuperscript{5-7}

"Clean Up" Behavior. For many field applications in production wells, oil productivity gradually increased or “cleaned up” during the first weeks after gel treatments were applied.\textsuperscript{7-9} To understand this phenomenon, we studied the dependence of oil and water permeabilities on throughput during various cycles of oil and water injection after gel or polymer placement in laboratory cores.
Behavior of a Cr(III)-Acetate-HPAM Gel

In our experiments, the gel contained 0.5% Ciba Alcoflood 935™ HPAM, 0.0417% Cr(III) acetate, 1% NaCl, and 0.1% CaCl₂ at 27°C. The hydrolyzed polyacrylamide polymer (HPAM) had a molecular weight of about 5x10⁶ daltons and a degree of hydrolysis of 5-10%. The first Berea sandstone core used was 7.6 cm long, with an absolute permeability of 746 md. Prior to gel injection, the core was flooded (with 3.34-cp hexadecane) to residual water saturation ($S_w=0.43$), where an endpoint permeability to oil ($k_o$) of 508 md was observed. Next, the core was flooded (with 0.93-cp brine) to residual oil saturation ($S_o=0.37$), where an endpoint permeability to water ($k_w$) of 120 md was measured. Then, 6 pore volumes (PV) of Cr(III)-acetate-HPAM gelant were injected, and the core was shut in to allow gelation. After gelation, hexadecane was injected using a fixed pressure gradient of 40 psi/ft. The green circles in Figure 1a demonstrate that permeability to oil increased gradually from 2 to 105 md during the course of 100 PV. The blue circles in Figure 1a show the permeability when water was injected after the above oil-injection stage. In contrast to the oil behavior, permeability to water stabilized at 0.17 md within a few tenths of one PV. During the second and third cycles of oil injection (yellow triangles and red squares in Figure 1b), permeability again gradually increased over the course of 100 PV. The permeability to oil followed the same trend for all three cycles (although the final permeability was 60% greater for the second and third cycles than for the first cycle). During the second cycle of water injection (blue triangles in Figure 1b), the permeability stabilized at 1.1 md within 1 PV.

1. Gel is placed in Berea sandstone core.
2. During oil flow after gel placement, $k_o$ rises from 2 to 105 md in 100 PV.
3. During water flow after gel placement, $k_w$ stabilizes at 0.17 md very quickly.

Figure 1a—Permeability to oil and water after gel placement in a Berea core.
Mobility Ratios
The concept of mobility ratio can explain the behavior in Figure 1. Mobility, \( k/\mu \), is defined as permeability of a porous material to a given phase divided by the viscosity of that phase. Mobility ratio, \( M \), is defined as mobility of the displacing phase divided by the mobility of the displaced phase.
Consider a case where water is injected into an oil zone to displace oil away from a well (Figure 2a), where oil and water viscosities and endpoint permeabilities are given in the previous section. As injected water displaces oil away from the wellbore, the “endpoint” mobility ratio is:

\[ M = \frac{(k_w/\mu_w)}{(k_o/\mu_o)} = \frac{120/0.93}{508/3.34} = 0.85(1) \]

Since \( M < 1 \), the displacement is stable, a fairly sharp “shock front” separates the mobile oil and water phases, and the permeability to water stabilizes fairly quickly (within 2 PV, as shown in Figure 2b).

Next, consider the mobility ratio when the well is returned to production, and oil displaces water toward the well:

\[ M = \frac{(k_o/\mu_o)}{(k_w/\mu_w)} = \frac{508/3.34}{120/0.93} = 1.2(2) \]

In this case, the mobility ratio is slightly greater than one, and therefore slightly unfavorable. However, the value is close enough to unity that the displacement is nearly piston-like. Consequently, the permeability to oil also stabilizes quickly (again, within 2 PV, as shown in Figure 2b).
Figure 2a—Stable displacements during water injection, followed by return to production (before gel placement).

Before gelant placement, oil and water permeabilities stabilized quickly.

Figure 2b—Rapid stabilization of $k_o$ and $k_w$ before gel placement.
Now, consider the case when a polymer solution or gelant is injected to displace either oil or water away from a production well (Figure 3). If the displacement is stable or near-stable before polymer or gelant injection, it is also stable during injection of polymer solutions or gelant, since these fluids are usually more viscous than water. (The notable exception occurs when the oil has a high viscosity.)

![Figure 3](image1)

**Figure 3**—Mobility ratios are usually favorable (stable displacement) during injection of gelant or polymer solutions.

After placement of the polymer solution or gelant and after gel formation, what happens when a well is returned to production? In the oil zone, oil with a relatively high mobility attempts to flow through gel which is basically immobile. Water can flow within the gel, although the permeability is very low. So, a mobility ratio can be estimated. For example, if \( k_o = 508 \text{ md at } S_{wr} \), \( \mu_o = 3.34 \text{ cp}, k_w = 0.17 \text{ md in the gel treated region, and } \mu_w = 0.93 \text{ cp} \), then the mobility ratio is \( (508/3.34)/(0.17/0.93) = 830 \). With this high unfavorable mobility ratio, the displacement is very inefficient, and oil forms wormholes through the gel treated region (Figure 4). For inefficient displacements, many pore volumes of throughput are required to achieve stabilization—just as observed during oil injection after gel placement (Figure 1). Concerning the formation of oil wormholes in the gel treated region, recognize that the oil cannot actually enter or flow through the gel polymeric structure. As oil pushes on the gel, water flows through the gel structure and exits the gel treated region at the wellbore. The pressure exerted by the oil on the gel causes some dehydration and the start of an oil pathway through the gel. As illustrated in Figure 4, this pathway becomes accentuated with time, resulting in a wormhole pattern.

![Figure 4](image2)

**Figure 4**—Unfavorable mobility ratio when an oil zone is returned to production after gel placement.
Finally, consider the case where a water zone is returned to production after gel placement (Figure 5). In this case, assume that the gel fills all aqueous pore space within the gel bank [as usually happens with our Cr(III)-acetate-HPAM gel]. On first consideration, we expect an unfavorable mobility ratio and an inefficient displacement similar to that illustrated in Figure 4. After all, water outside the gel treated region is much more mobile than water inside the gel treated region. However, in contrast to the oil, water can actually enter and flow through the gel structure. Upon entry, this water immediately becomes part of the gel. No gel dehydration occurs, no wormhole pathways form, and the displacement remains stable. The gel remains in exactly the same location, but water just flows through the gel, experiencing a very low permeability. So, the effective permeability to water stabilizes rapidly, as observed in Figure 1.

![Figure 5—Stable displacement when a water zone is returned to production after gel placement.](image)

In summary, the concepts of mobility ratio and stable versus unstable displacement explain the behavior in Figure 1.

**Permeability to Water during Many Experiments**

**Typical Behavior.** Table 1 lists stabilized final permeability to water after gel placement for many experiments using the Cr(III)-acetate-HPAM gel. Three porous media were examined, including strongly water-wet Berea sandstone and fused silica and strongly oil-wet porous polyethylene. Initial core permeabilities ranged from 738 to 15,270 md. Most cores were 7.6 cm long, although two Berea cores were 15.2 cm long. The pressure gradient applied ranged from 10 to 100 psi/ft. The $k_w$ values were measured under several different conditions, including (1) when water was the first fluid injected after gel placement, (2) when oil was the first fluid injected after gel placement and then followed by water injection, and (3) when at least one cycle of water and oil were injected before the $k_w$ measurement.

<table>
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<tr>
<th>Core</th>
<th>Core length, cm</th>
<th>Initial core $k$, md</th>
<th>$dp/dl$, psi/ft</th>
<th>Condition</th>
<th>$k_w$ at $S_{or}$ after gel, md</th>
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<td>850</td>
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<td>water 1&lt;sup&gt;st&lt;/sup&gt;</td>
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Average $k_w$ for five “water first” cases: 0.26 md (± 0.1 md)
(Excluding 100 psi case in silica); PE = polyethylene

For most cases in Table 1, permeability to water stabilized at the reported value within one PV and remained stable for up to 100 PV. For five cases where water was the first fluid injected after gel placement, permeability to water averaged 0.26 md. This value was of the order expected if all aqueous pore space was filled with gel and water only flowed through the gel.\(^\text{10}\)

**Breakdown after High Pressure Gradients.** For several cases flooded at 100 psi/ft (end of Table 1), $k_w$ values were high (up to 211 md), suggesting significant gel breakdown at this high pressure gradient. This breakdown had an impact on the time required for stabilization of permeabilities during water injection. From the blue circles in Figure 6, a case is shown where $k_w$ steadily increased during the course of injection 100 PV of water. Why did $k_w$ not stabilize quickly as in show by the blue circles in Figure 1. In contrast to the explanation associated with Figure 5, the displacement during water injection appears unstable. This behavior is more consistent with the behavior illustrated by Figure 4. Presumably, the unstable displacement occurred because the gel breached by the water at 100 psi/ft.
For cases where at least one cycle of oil preceded the $k_w$ measurement, permeability ranged from 0.17 to 211 md, but were commonly between 1 and 3 md (Table 1).

**Stability of $k_w$ with Time.** An experiment was performed to test how persistently the gel would reduce permeability during continuous water flow. A porous polyethylene core (6.4 cm long, 3.8 cm diameter) was saturated with our standard Cr(III)-acetate-HPAM gel [0.5% Alcoflood 935, 0.0417% Cr(III) acetate, 1% NaCl, 0.1%CaCl$_2$]. After gelation, brine (1% NaCl, 0.1%CaCl$_2$) was allowed to flow through the gel-filled core using a constant pressure gradient of 30 psi/ft. This pressure gradient was established by placing a 442-cm high column of brine over the core. Figure 7 shows the results. Over the course of eight months, the permeability to water remained fixed at about 60 µd. This experiment will be continued to assess how long the permeability to water remains stable.
Modeling of $k_o$ and $k_w$ Behavior

The trends observed in Figure 1 can be matched quite well using conventional relative permeability equations.\textsuperscript{14} The permeability equations shown in Figure 8, along with the listed parameters for endpoint permeabilities, saturations, and viscosities, were used to predict $k_o$ versus oil throughput (yellow curve) and $k_w$ versus water throughput (dark blue curve). The code used for the modeling work can be viewed in Appendix A of Ref. 15.

Figure 7—Permeability to brine versus time.
Permeability to Oil during Many Experiments

**Typical Behavior.** In contrast to the behavior during water injection, the apparent permeability steadily increased during injection of 100 PV of oil. Figure 9 shows overall core $k$ versus PV during oil injection for many experiments (performed with those in Table 1). The green curve in Figure 9 shows predictions when 3-cp oil (with endpoint $k_o=100$ md) was injected into a core (at $S_{or}$ after gel placement) where 1-cp water had an endpoint $k_w=0.26$ md. For the white curve, endpoints $k_o=1,000$ md and $k_w=1$ md. (In both cases, $S_{or}=0.368$ and $S_{wr}=0.432$.) The two curves provide lower and upper limits of behavior for the Cr(III)-acetate-HPAM gel. The dashed purple curve provides an intermediate case where endpoints $k_o=400$ md and $k_w=0.4$ md.

\[
k_o = k_{o \text{ at } Swr} \left[ \frac{(1-S_w-S_{or})}{(1-S_{wr}-S_{or})} \right]^2
\]
\[
k_w = k_{w \text{ at } Sor} \left[ \frac{(S_w-S_{wr})}{(1-S_{wr}-S_{or})} \right]^2
\]

$k_o \text{ at } Swr = 160$ md, $k_{w \text{ at } Sor} = 0.17$ md

$S_{or} = 0.368$, $S_{wr} = 0.432$

$\mu_O = 3.34 \text{ cp}$, $\mu_w = 0.93 \text{ cp}$

Figure 8—Model predictions versus experimental data.
Minimun Pressure Gradient for Oil Flow. In the above experiments, the lowest pressure gradient used was 10 psi/ft. We wondered whether a minimum pressure gradient existed, below which oil would not penetrate through the gel. After placement of Cr(III)-acetate-HPAM gel in an 8-darcy polyethylene core, oil was used to apply pressure gradients of 0.43 psi/ft for 6 days, followed by 0.86 psi/ft for 10 days, and 1.3 psi/ft for 15 days. No flow was detected (i.e., $k_o < 1 \mu d$). Oil flow was finally observed after the pressure gradient was raised to 1.7 psi/ft. Therefore, in this polyethylene core, the minimum pressure gradient needed to initiate oil flow was between 1.3 and 1.7 psi/ft.
Predicting Oil-Zone Clean-up for Field Applications

How quickly will oil productivity increase after a gel treatment where gelant invaded the oil productive zones? This question can readily be answered using a simple mobility ratio model, where the key input parameters are endpoint $k_w$ and $k_o$. Appendixes B and C of Ref. 15 list the model code for the predictions presented in this section. In these examples, the external drainage distance or radius was 500 ft, $S_{or}=0.368$, and $S_{wr}=0.432$. For radial cases, the wellbore radius was 0.5 ft. The first predictions assumed that the oil residual resistance factor ($F_{rro}$) in the gel-treated region approached unity after a large volume of oil throughput (i.e., $k_o$ at $S_{wr}$ was the same in gel-treated and untreated rock). In the following figures, time (during flow) is plotted on the $x$-axis, while the $y$-axis plots oil productivity (i.e., the oil productivity index) relative to the oil productivity if no gel treatment had been applied.

**Effect of Distance of Gelant Penetration.** Figures 10 and 11 show the influence of distance of gelant penetration on the recovery time for oil productivity for fractured (linear flow) and unfractured (radial flow) production wells. Pressure drawdown ($\Delta p$, between the external drainage distance and the wellbore) was fixed at 100 psi. As expected, the time for oil “clean-up” increased significantly with increased distance of gel penetration. For both fractured and unfractured cases, gelant penetration distances less than 10 ft provided the most desirable times to recover oil productivity (i.e., a day or less). Caution: for large distances of gelant penetration, the pressure gradient may be too low (e.g., <1.7 psi/ft) to allow oil to initiate flow through the gel (see the previous section).

![Time to regain oil productivity versus distance of gelant leakoff in fractured wells.](image)

*Figure 10—Effect of distance of gel penetration from a fracture face.*
Based on Figures 10 and 11, Figure 12 was prepared, showing the time for a well to regain 50% of its original oil productivity. Recovery times were similar for linear and radial flow. Clean-up time ($t$) varied with the cube of gel penetration ($L_p$).
Clean up time increases with distance of gelant penetration to the third power.

Figure 12—Clean-up time in linear versus radial flow.

**Effect of Pressure Drawdown.** The time for clean-up of an oil zone varied inversely with pressure drawdown. Increasing the pressure drawdown from 1 to 1,000 psi decreased the clean-up time 1,000-fold (solid curves in Figure 13). For unfractured wells where the radius of gelant penetration was 10 ft, relatively high pressure drawdowns were needed to clean up the oil zones in a reasonable time period. For gel treatments in fractured production wells where the distance of gelant leakoff from fracture faces was relatively small, oil zones cleaned up quickly even for low drawdowns (symbols in Figure 13).
Figure 13—Effect of pressure drawdown on oil-zone clean-up.

Figure 14 emphasizes the inverse relation between clean-up time and pressure drawdown.
Effect of $k_w$ and $k_o$. The time for clean-up of an oil zone varied inversely with the endpoint $k_w$ after gel formation, but was not sensitive to the endpoint $k_o$ (Figure 15). Clean-up time decreased by a factor of 100 as $k_w$ increases from 0.1 to 10 md (when $k_o$ was held constant at 1,000 md). In contrast, when $k_w$ was held constant at 0.26 md, the clean-up time was basically unaffected as $k_o$ increased from 100 to 10,000 md.

Note that the white and yellow solid curves in Figure 15 show predictions associated with lower and upper limits that bracket the data in Figure 9. These data suggest a maximum four-fold variation in clean-up time for the experiments in Figure 9.
Summary. In this analysis, the time to restore productivity to a gel-treated oil zone was (1) similar for radial and linear flow, (2) proportional to the cube of distance of gel penetration, (3) inversely proportional to pressure drawdown, (4) inversely proportional to the endpoint $k_w$ at $S_{or}$ in the gel-treated region, and (5) not sensitive to the endpoint $k_o$ at $S_{wr}$.
Effect on Ultimate Oil Productivity

Although $k_o$ at $S_{wr}$ (after gel placement) has no effect on the clean-up time (Figure 15), it does impact how much of the original oil productivity can ultimately be regained after a gel treatment. In the above analysis, we assumed that the permeability to oil in the gel-treated region would eventually approach $k_o$ at $S_{wr}$ in the untreated region. What happens if permeability to oil in the gel-treated region cannot rise to match the original $k_o$?

Productivity reduction from a gel treatment is described by Eq. 3 for linear flow and by Eq. 4 for radial flow:

\[
\frac{q}{q_o} = \frac{L_e}{[(F_{rr} - 1) L_p + L_e]} \quad \text{.................................. (3)}
\]

\[
\frac{q}{q_o} = \frac{\ln(r_e/r_w)}{[(F_{rr} \ln(r_p/r_w) + \ln(r_e/r_p)]} \quad \text{......... (4)}
\]

In these equations, $q/q_o$ is the ultimate productivity relative to productivity before the gel treatment; $r_e$ is the external drainage radius; $L_e$ is the external drainage distance; and $r_w$ is the wellbore radius. In our examples, $L_e = r_e = 500$ ft and $r_w = 0.5$ ft. $F_{rr}$ is the ultimate or stabilized residual resistance factor (i.e., the factor by which the permeability to oil or water is reduced by the gel). Figures 16 and 17 show results of ultimate productivity calculations for linear and radial flow. These figures are applicable to either oil or water flow.

Figure 16—Ultimate productivity after gel placement in a fractured production well.
In radial flow, productivity loss is much more sensitive to $F_{rr}$ than to radius of gel penetration.

Figure 17—Ultimate productivity after gel placement in an unfractured production well.

Gel Penetration from Fracture Faces. Figure 18 simplifies Figure 16 by plotting $(F_{rr} - 1)L_p$ on the x-axis. To maintain high oil productivity in a fractured well, the x-axis parameter should be less than 100 ft (and preferably less than 40 ft). To maintain low water productivity, the x-axis parameter should be greater than 3,000 ft. These objectives can be achieved by controlling $F_{rr}$ or the distance of gel penetration ($L_p$) or both.
In linear flow, productivity loss is equally sensitive to $F_{rr}$ and distance of gel penetration.

Figure 18—Ultimate productivity after gel placement: linear flow, simplified correlation.

What range of oil residual resistance factors ($F_{rrn}$) occurred with the Cr(III)-acetate-HPAM gel? In Berea, $k_o$ at $S_{wr}$ before gel placement typically was about 500 md (Figure 2b). Given the lower-limit curve in Figure 9, the lower limit of $k_o$ at $S_{wr}$ after gel placement (after many PV of oil throughput) was 100 md. For this case, $F_{rrn}$=5 (500/100). From Figure 18, a high ultimate oil productivity would be retained [i.e., $(F_{rr} - 1)L_p < 40$ ft] if the distance of gel penetration was less than 10 ft [i.e., 40/(5-1)]. For some experiments (Figure 9), the permeability to oil in Berea (after gel) exceeded 300 md and the ultimate permeability approached $k_o$ at $S_{wr}$ for the untreated rock. In these cases, $F_{rrn}$<2, and the maximum acceptable distance of gel penetration (from the fracture faces) could be 40 ft or more.

Higher oil resistance factors and lower acceptable distances of gel penetration were noted for the polyethylene and fused silica cores. In polyethylene, $k_o$ at $S_{wr}$ typically was between 5 and 10 darcys before gel placement, depending on the initial (absolute) permeability of the core. Given these values and the $k_o$ values from Figure 8, $F_{rrn}$ values could range from 5 to 77 (i.e., 5,000/1,000 to 10,000/130). If $F_{rrn}$=77, the maximum allowable gel penetration (from Figure 17) is 0.5 ft [i.e., 40/(77-1)].

A similar analysis can be performed for the fused silica data. Here, $k_o$ at $S_{wr}$ was typically about 1,000 md before gel placement. Ultimate $F_{rrn}$ values could range from 2 to 5, and a conservative maximum allowable gel penetration would be 10 ft from the fracture faces [i.e., 40/(5-1)]. Our analysis in the previous section (white curve in Figure 9) indicated that restoration of oil productivity should occur fairly quickly if gel penetration is less than 10 ft.
The above analysis focused on gel penetration into an oil zone. Of course, in addition to minimizing damage to oil productivity, a gel treatment should substantially reduce water productivity.\textsuperscript{5-7} As mentioned, the parameter, \((F_{rr} - 1)L_p\), should be greater than 3,000 ft in the water zone. To assess the appropriate distances of gel penetration, the water residual resistance factor, \(F_{rrw}\), is needed. In turn, determining \(F_{rrw}\) requires knowledge of \(k_w\) at \(S_{or}\) before and after gel placement. Before gel placement, \(k_w\) at \(S_{or}\) was 120 md in Berea, 4,000-6,500 md in polyethylene, and 140-640 md in fused silica. If \(k_w = 0.26\) md at \(S_{or}\) after gel placement, \(F_{rrw}\) was 460 in Berea, 15,000-25,000 in polyethylene and 540-2,400 in fused silica. Achieving a \((F_{rr} - 1)L_p\) parameter of 3,000 ft requires \(L_p \geq 6.5\) ft in Berea. Smaller distances of gel penetration would be acceptable in the other porous media.

To summarize the significance of the above calculations, consider a vertical production well with a two-wing vertical fracture that cuts through one oil zone and one water zone. Assume that both zones are Berea sandstone where \(k_w = 120\) md at \(S_{or}\) and \(k_o = 508\) md at \(S_{ow}\) before placement and \(k_w = 0.26\) md at \(S_{or}\) after placement of the Cr(III)-acetate-HPAM gel. This analysis suggested that the optimum distance of gel penetration from fracture faces should be at least 6.5 ft in the water zone but less than 10 ft in the oil zone. Of course, these distances apply only to this particular circumstance. The calculations must be repeated if the circumstances or input parameters are different.

**Gel Penetration in Unfractured Wells.** We advocate that hydrocarbon zones must be protected during gel placement in unfractured wells with radial flow.\textsuperscript{1,2} However, upon observing the degree of clean-up during oil flow through gel (Figures 1 and 9), we wondered whether exceptions might be found to our earlier beliefs. Close consideration of Figure 17 indicates that for gel radii greater than 3 ft, oil residual resistance factors must be less than 2 to insure minimum loss of oil productivity. This observation is consistent with our earlier findings.\textsuperscript{1,2} Can \(F_{rro}\) values less than 2 be achieved reliably with the Cr(III)-acetate-HPAM gel? The discussion after Figure 18 indicated that ultimate \(F_{rro}\) values might range from 1 to 5 in Berea, 2 to 5 in fused silica, and 5 to 76 in polyethylene. With the variations observed, it still seems unduly risky to inject gelant into unfractured wells without protecting the hydrocarbon zones from gel damage.

**Behavior of an Adsorbed Polymer**

The above work used a Cr(III)-acetate-HPAM gel that fills all aqueous pore space. Berea cores treated with an adsorbing polymer (i.e., solutions containing 0.18% BJ AquaCon™, 2% KCl) also exhibited permeabilities that increased gradually during the course of injecting 100 PV of oil.\textsuperscript{16} In contrast to the Cr(III)-acetate-HPAM gel, this polymer did not occupy very much of the aqueous pore space and provided low water and oil residual resistance factors. Figure 19 shows how permeabilities to oil and water both experienced gradual increases during the course of injecting 100 PV of fluid after polymer placement. These results suggest unstable displacements during both oil and water injection. The explanation for the throughput dependence of \(k_o\) remains the same as that given for oil flow after placement of the Cr(III)-acetate-HPAM gel. However, why did \(k_w\) also show a gradual increase? Since the adsorbed polymer occupies only a small fraction of the aqueous pore space, water flows around the gel as well as through the gel. This fact allows for the formation of viscous fingers or wormholes during displacement of oil by water (i.e., an unstable displacement). In constrast, recall for the Cr(III)-acetate-HPAM gel (that filled all aqueous pore space), water was forced to flow only through the gel, so no viscous fingers or wormholes could form (because water that entered the gel became part of the gel).
For this adsorbing polymer in Berea, Figure 19 shows how permeability to oil increased with throughput for six experimental cases. In two cases (yellow triangles and green squares), oil was the first fluid injected after polymer placement. In these two cores, water was subsequently injected, followed by an additional cycle of oil (red circles and purple squares). In two other cases (and separate cores), water was injected first after polymer placement, followed by oil injection (blue circles and white diamonds).

The thin and thick curves in Figure 20 plot predictions from our model. The endpoint $k_o$ and $k_w$ input values used to generate the curves are indicated in Figure 20. These curves did a reasonable job of bracketing the experimental data. However, the general shapes of the model curves did not follow the data trends as well as those for Cr(III)-acetate-HPAM gels (Figure 9). The upper and lower curves were separated by a factor of seven in Figure 9 and a factor of two in Figure 20. As throughput increased from 1 to 100 PV, oil permeability increased typically by 5 to 10 in Figure 9 and by 2 to 3 in Figure 20.
Figure 20—Permeability during oil injection after treatment with an adsorbing polymer.

Ultimate oil residual resistance factors (after 100 PV) ranged from 1.4 to 2.1 for the experiments in Figure 20. On first consideration, these values might seem attractive for field applications—especially in unfractured wells (see Figure 17). Unfortunately in these cases, water residual resistance factors were roughly the same as the oil residual resistance factors. (Water residual resistance factors and final permeability to water after polymer placement are listed in Table 2.) Consequently, within the variability of the experimental results, a polymer treatment would reduce productivities of oil and water zones by roughly the same factor.

In contrast to the behavior of the Cr(III)-acetate-HPAM gel, after treatment with the polymer, permeability to water often increased steadily over time. This behavior could be caused by erosion or desorption of the polymer. Erosion or desorption of the polymer could also explain the difference between the model predictions and the oil experimental data in Figure 20. At high throughput values, the model predicts that permeability to oil should level off, whereas the actual data continue to follow the same increasing trend—consistent with expectations for erosion or desorption.

<table>
<thead>
<tr>
<th>Condition</th>
<th>Initial core $k$, md</th>
<th>$k_w$ at $S_{or}$, (before gel), md</th>
<th>$k_w$ at $S_{or}$, (after gel), md</th>
<th>$F_{rw}$</th>
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In summary, after placement of an adsorbing polymer (AquaCon) in Berea, the permeability to oil increased significantly over the course of 100 PV. The polymer also provided fairly low oil residual resistance factors. Unfortunately, the polymer provided correspondingly low water residual resistance factors. If water residual resistance factors are too low, insufficient reduction in water productivity may be realized in field applications.\textsuperscript{1,2,5} For polymers and gels that provide similar residual resistance factors to oil and water, with values greater than two, hydrocarbon zones should be protected during gel placement.\textsuperscript{1,2}

<table>
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<th>1\textsuperscript{st}</th>
<th>2\textsuperscript{nd}</th>
<th>1\textsuperscript{st}</th>
<th>2\textsuperscript{nd}</th>
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<td>38</td>
<td>469</td>
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<tr>
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<td>853</td>
<td>93.3</td>
<td>469</td>
<td>95.5</td>
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<tr>
<td>water 1\textsuperscript{st}</td>
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<td>84.4</td>
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</table>
Note on Field Applications
In this paper, formation damage during a treatment was assumed to be caused by only gel or polymer. The application of a gel or polymer treatment was also assumed to not stimulate (increase) hydrocarbon or water injectivity indexes. However, field cases have been reported (in the Arbuckle formation\textsuperscript{17}) where gel treatments dramatically increased the oil productivity index. How could this happen? One possible explanation is as follows: When gelant or gel was injected into a production well, the downhole pressure was necessarily greater than at any time during production. If the well intersected fractures (either natural or artificially induced), the relatively high pressure during gel placement could force open the fracture or fracture system—thus stimulating the well and explaining why oil increased significantly. Why did the water productivity index not increase as well? Presumably, the explanation lies in the disproportionate permeability reduction provided by the gel. Opening the fracture system acted to stimulate both oil and water productivity, while gel in the matrix (of oil and water zones that were cut by the fracture) acted to diminish both oil and water productivity. The ultimate productivity index was determined by the relative importance of (1) increased fracture area from pressurizing the well versus (2) the damage caused by the gel to the fracture areas in the oil and water zones. If the water residual resistance factor was sufficiently high, the water productivity index decreased even though the fracture area was increased during the treatment. If the oil residual resistance factor was sufficiently low, the oil productivity index increased even though the oil zone was damaged somewhat by the gel.

If the fracture area open to flow is changed by application of a polymer or gel treatment, that change must be quantified before predicting clean-up of oil productivity with our method.
Conclusions
The oil and water throughput requirements for stabilization of permeabilities were studied for a relatively “strong” pore-filling Cr(III)-acetate-HPAM gel and for a “weak” adsorbing polymer in cores. The following conclusions were reached:

1) As oil throughput increased from 1 to 100 PV, permeability to oil gradually increased by factors from 5 to 10 for cores treated with the Cr(III)-acetate-HPAM gel and from 2 to 3 for cores treated with the adsorbing polymer.
2) After treatment with Cr(III)-acetate-HPAM gel, permeability to water stabilized rapidly and remained stable for over eight months. In contrast, after treatment with the adsorbing polymer, permeability to water often increased steadily over time—possibly due to erosion or desorption of the polymer.
3) After placement of Cr(III)-acetate-HPAM gel in a 8-darcy polyethylene core, the minimum pressure gradient to initiate oil flow was between 1.3 and 1.7 psi/ft.
4) A simple mobility-ratio model predicted clean-up times for both fractured and unfractured wells after a gel treatment. The time to restore productivity to a gel-treated oil zone:
   a) was similar for radial versus linear flow,
   b) varied with the cube of distance of gel penetration,
   c) varied inversely with pressure drawdown,
   d) varied inversely with $k_w$ at $S_o$, in the gel-treated region,
   e) and was not sensitive to the final $k_o$ at $S_w$.
5) Although $k_o$ at $S_{wr}$ (after gel placement) had no effect on the clean-up time, it strongly affected how much of the original oil productivity could ultimately be regained.
6) Consistent with earlier work, the new results and analysis confirmed that in radial matrix flow (e.g., unfractured wells), hydrocarbon productive zones must be protected during gelant or polymer placement.
Nomenclature

\[ F_{rr} = \text{residual resistance factor (mobility before gel divided by mobility after gel)} \]
\[ F_{rro} = \text{oil residual resistance factor} \]
\[ F_{rrw} = \text{water residual resistance factor} \]
\[ k = \text{permeability, md} \left[ \mu m^2 \right] \]
\[ k_o = \text{permeability to oil, md} \left[ \mu m^2 \right] \]
\[ k_w = \text{permeability to water, md} \left[ \mu m^2 \right] \]
\[ k/\mu = \text{mobility, md/cp} \left[ \mu m^2/mPa-s \right] \]
\[ (k/\mu)_o = \text{oil mobility, md/cp} \left[ \mu m^2/mPa-s \right] \]
\[ (k/\mu)_w = \text{water mobility, md/cp} \left[ \mu m^2/mPa-s \right] \]
\[ L_e = \text{external drainage distance, ft [m]} \]
\[ L_p = \text{distance of gelant penetration, ft [m]} \]
\[ M = \text{mobility ratio} \]
\[ \Delta p = \text{pressure drop, psi [Pa]} \]
\[ q = \text{injection or production rate after gel placement, BPD} \]
\[ q_o = \text{injection or production rate before gel, BPD} \]
\[ r_e = \text{external drainage radius, ft [m]} \]
\[ r_{gel} = \text{radius of gelant penetration, ft [m]} \]
\[ r_p = \text{radius of gelant penetration, ft [m]} \]
\[ r_w = \text{wellbore radius, ft [m]} \]
\[ S_{or} = \text{residual oil saturation} \]
\[ S_w = \text{water saturation} \]
\[ S_{wr} = \text{residual water saturation} \]
\[ t = \text{time, d} \]
References